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# Learning restrictive analyses of Canadian Raising in OT <br> using exceptionality diacritics 

## Aleksei Nazarov <br> Utrecht University

## Opacity (restrictive analysis)

- Canadian English: low diphthongs/ai av/ raise before:
- Voiceless consonants (transparent)
rııt 'write', mıus 'mouse'
- Voiced [r] only if derived from /t/ ("overapplication" opacity) (opaque)
rair ${ }^{\prime}$ 'writer' ( $\leftarrow$ rait- $\boldsymbol{\prime}$ )
BUT rair $\boldsymbol{\circ}^{\prime}$ 'rider' ( $\leftarrow$ raid- $\boldsymbol{\text { r }}$ )
- Restrictive analysis of such an opaque pattern:
- Ensures no word has unraised diphthong + voiceless C
*klart
- Ensures no word has raised diphthong + voiced $C \nleftarrow / t /$



## Serial vs. Parallel analyses

- Serial analysis (traditional; Chomsky 1964, Bermudez-Otero 2003):

1. Raising applies before voiceless consonants
2. t is "flapped" $(\rightarrow \mathrm{r})$ in certain $\vee \_\vee$ environments
> Learnable (Nazarov \& Pater 2017), but reintroduces serialism into Optimality Theory (Prince \& Smolensky 1993/2004)

- Parallel analysis that acknowledges phonological opaque interaction (cf. Hayes 2004, Pater 2014) and does not assume extra representational levels (cf. Boersma 2007):
- Raising applies before consonants indexed $i$ (Pater 2000, Round 2017)
- Consonants indexed $i$ are either voiceless, or flaps derived from /t/ (see next slide)
> Avoids conceptual disadvantages, but is it learnable? Under which circumstances?
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## Local indexation analysis

- Indexed constraints only apply to items marked by a particular index (Pater 2000, 2010)
- Round (2017): individual segments may have an index
- Indices stay the same between input and output (cf. Chomsky \& Halle 1968)
- Restrictive analysis of Canadian Raising:

| $/ \mathrm{bab} /$ | ${ }^{*}[+ \text { voice }]_{\mathrm{i}}$ | $*[+$ voice $]$ |
| :--- | :--- | :--- |
| bab |  | $* *$ |
| $/ \mathrm{b}_{\mathrm{i}} \mathrm{ab} /$ |  |  |
| $\mathrm{b}_{\mathrm{i}} \mathrm{ab}$ | $*$ | $* *$ |

- No consonant indexed $\boldsymbol{i}$ follows an unraised diphthong

$$
{ }^{*} \mathrm{C}_{\mathrm{i}} / \mathrm{aI}_{-} \gg \operatorname{Ident}(\text { low }) \quad *_{\text {rait }}^{\mathrm{i}}, \sqrt{ }, \sqrt{ } \mathrm{rIt}_{\mathrm{i}}
$$

- Segments indexed $\boldsymbol{i}$ must be voiceless by default

$$
\text { *[+voice }]_{\mathrm{i}} \gg \text { Ident(voice) }
$$

- Except when flapping applies: it turns $\boldsymbol{i}$ segments voiced

$$
*_{\mathrm{r}_{0}}, * \mathrm{~V}\{\mathrm{t}, \mathrm{~d}\} \mathrm{V} \gg *[+ \text { voice }]_{\mathrm{i}} \gg \text { Ident(voice), Ident(son) }
$$

$$
\begin{aligned}
& \checkmark \text { rAIf }{ }^{i} \text { a }
\end{aligned}
$$

## Learning (local) indexation

- To learn indexation analysis:
- Start with universal constraints and unindexed inputs
- Determine which constraints \& which input segments have which index
- Rank all constraints
- Here: Round's (2017) algorithm:
- Operates within Biased Constraint Demotion (BCD; Prince \& Tesar 2004)
- When BCD gets stuck, finds most generally applicable indexed constraint \& corresponding indexed segments - add constraint to analysis and continue BCD (cf. Pater 2010)
- Algorithm categorical, but makes random guesses when it cannot decide between analyses based on the data


## Simulation setup

- Three data sets (what does learner need to see?):

| Constraints used: |
| :---: |
| *[+voice], *[-voice] |
| *aI, *${ }_{\text {II }}$ |
| *C/ar_, *C/ar_ |
|  |
|  |
| *V $\{t, d\} \mathrm{V}$ |
| Ident (voice) |
| IDENT(son) |
| IDENT (low) |


| $D_{1}$ <br> (no transparent CR) |
| :---: |
| [flıirə ${ }^{\text {] }}$ 'flighter' |
| [glairə'] 'glider' |
| [saıə] 'sigher' |
| [vaıə] 'vier' |


| $D_{2}$ |  |
| :--- | :--- |
| (transp | CR, no alternations) |
| flıIrə | flııt |
| glaırə | glaid |
| saıə | sai |
| vaıə | vai |

- Three UR hypothesis sets (what does learner need to assume?):

| UR ${ }_{1}$ <br> (all surf cands = URs) | $\mathrm{UR}_{2}$ (uncertainty wrt voicing) | $\mathbf{U R}_{3}$ (canonical URs only) |
| :---: | :---: | :---: |
| $I\left\{\begin{array}{l} \mathrm{f} \\ \mathrm{v} \end{array}\right\}\left\{\begin{array}{l} \mathrm{l} \\ 0 \\ \mathrm{l} \end{array}\right\}\left\{\begin{array}{l} \mathrm{a} \\ 1 \end{array}\right\}\left[\begin{array}{l} \mathrm{t} \\ \mathrm{~d} \\ \mathrm{~d} \\ 0_{0} \\ \mathrm{r} \end{array}\right\} \sigma$ | $/ \text { fla }\left\{\begin{array}{l} \mathrm{t} \\ \mathrm{~d} \end{array}\right\} \sigma \sigma /$ | /flaitar |

## Results

- For each condition (data set x UR hypothesis), 20 runs
- All runs lead to some consistent analysis of the data
- Table: number of times restrictive analysis is found for each condition

|  | UR 1 : all surf cands = URs | UR $_{2}$ : uncertainty wrt voicing | UR $_{3}$ : "correct" URs |
| :--- | :--- | :--- | :--- |
| $\mathrm{D}_{1}$ : no transparent CR | 0 | 0 | 0 |
| $\mathrm{D}_{2}$ : transp CR, no alternations | 0 | 0 | 0 |
| $\mathrm{D}_{3}$ : transp CR and alternations | $15(/ 20)$ | $7(/ 20)$ | 0 |

- Restrictive analysis found for dataset $D_{3}$ and $U R_{1} / \cup R_{2}$
- True alternation between t and r necessary
- Uncertainty about UR of $[t \sim r]$ necessary (present in $\mathrm{UR}_{1} / \mathrm{UR}_{2}$ but not in $\mathrm{UR}_{3}$ )


## Discussion \& Conclusion

- Learning indexation analysis of Canadian Raising: possible - Based on Round's (2017) segmentally local indexation learner
- Conditions:
- learner has access to transparent instances of process and alternations
- learner has not yet finished determining URs of crucial segments
- Possible to analyze at least this case of opacity without serialism (cf. McCarthy 2007) and without additional levels of representation (cf. Boersma 2007)
- This analysis is learnable and discoverable from data given a universal constraint set
- Other types of opacity? Probabilistic learner? Other assumptions about URs, data, constraints, etc.?


## Thank you!

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Although every effort has been made to ensure that all information in this presentation is correct and up to date, Utrecht University cannot be held liable for any false, inaccurate or incomplete information presented herein.

## Appendix

## Indexation

- Indexation: universal constraints may have variants specific to some inputs (morphemes/words) only (Pater 2000)
*[+voice]: no voiced segments
*[+voice] $]_{i}$ : no voiced segments in $i$ words
- Extended indexation: indices are local to specific segments (Round 2017) and represented as binary; basically same as SPE diacritics
${ }^{*}[+ \text { voice }]_{[+i]}$ : no voiced [+i] segments
$\checkmark[\mathrm{d}]_{[-i]} \quad *[\mathrm{~d}]_{[+\mathrm{i}]}$


## Canadian Raising with indexation

- Raising: ${ }^{*} \mathrm{C}_{[+\mathrm{i}]} /$ aI_ >> Ident(low)

| /גart[+i]/ | ${ }^{*} \mathrm{C}_{[+1]} / \mathrm{Ia}_{-}$ | Id(low) |
| :---: | :---: | :---: |
| [ artit $\left._{[+i]}\right]$ | *! |  |
| $\cdots\left[\wedge \wedge t_{[+i]}\right]$ |  | * |

All underlying segments are [-i] unless specified otherwise

- Flapping: $* V\{t, \mathrm{~d}\} \mathrm{V} \gg{ }^{*}[+ \text { voice }]_{[+j \mathrm{j}}$, Ident(son), Ident(voi)

| /bat[+i]ə/ | * V t, d\} V | ${ }^{[ }+$voice] $]_{\text {[ii] }}$ | Id(son) | Id(voi) |
| :---: | :---: | :---: | :---: | :---: |
| [bstt ${ }_{[+1]}$ ] $]$ | *! |  |  |  |
| $\cdots\left[\mathrm{b} \wedge[+i]^{2}\right]$ |  | * | * | * |

## Canadian Raising with indexation

- The surface voicing of a [+i] segment does not influence raising

| /」art[+i]-2/ | *V\{t,d\}V | *[+voice] ${ }_{[+i]}$ | $* C_{[+i]} / \mathrm{aI}_{-}$ | Ident(low) | Ident(son) | Ident(voi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| daIt $_{[+ \text {ij }}{ }^{2}$ | *! |  | + |  |  |  |
| $1 \wedge \mathrm{It}_{[+\mathrm{i}]} \gamma$ | *! |  | , | * |  |  |
| $\operatorname{saId}_{[+i]} 2$ | *! | * | \| |  |  | * |
| $1 \wedge \mathrm{Id}_{[+i]}{ }^{2}$ | *! | * | \| | * |  | * |
| $\operatorname{laIr}_{[+i]}{ }^{2}$ |  | * | $\left.\right\|^{*}$ ! |  | * | * |
|  |  | * | , | * | * | * |

All segments are [-i] unless specified otherwise

## Richness of the Base

- Anything with [+i] always shows up as voiceless and triggers raising unless it's in the flapping context

| /ard[+i]/ | *V\{t,d\}V | *[+voice $]_{[+i]}$ | $*[\text {-voice }]_{[-i]}$ | ${ }^{*} \mathrm{C}_{[+\mathrm{i}]} / \mathrm{ar}$ | Ident(low) | Ident(son) | Ident(voi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| aIt |  |  |  | \| * |  |  | ! * |
| AIt |  |  |  |  | * | \| | , * |
| aid |  | *! |  | * |  |  |  |
| AId |  | *! |  | I | * | I | I |
| aIr |  | *! |  | * |  | * | I |
| MIS |  | *! |  | ! | * | ! * | 1 |

All underlying segments are [-i] unless specified otherwise

## Richness of the Base

- Anything with [-i] always shows up as voiced and never triggers raising

| /art[-i]/ | *V\{t, d\}V | *[+voice] $]_{[+i]}$ | $\left.{ }^{[- \text {voice }}\right]_{[-\mathrm{ij}}$ | ${ }^{*} \mathrm{C}_{[+\mathrm{i}]} / \mathrm{aI}$ | Ident(low) | Ident(son) | Ident(voi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| art |  |  | *! |  |  |  |  |
| AIt |  |  | *! |  | * |  |  |
| ${ }^{6}$ ard |  |  |  |  |  |  | * |
| AId |  |  |  |  | *! |  | * |
| air |  |  |  |  |  | *! |  |
| Mir |  |  |  |  | *! | 1* | * |

All underlying segments are [-i] unless specified otherwise

## Round's (2017) learner in more detail

- Round (2017): model to learn segmentally local indexation from winner-loser pair data

1. Based on Biased Constraint Demotion (BCD, Tesar and Smolensky 2004)
2. Whenever two inputs in the data have conflicting ranking requirements (= inconsistency): induce some indexed constraint (Pater 2010)
3. Which indexed constraint assigned to which segments? (new contribution) Selected based on number and location of Winner-preferring violation loci

## Biased Constraint Demotion

- Version of Recursive Constraint Demotion (Tesar 1995) with a Markedness-over-Faithfulness bias
- Start with no ranking
- At each step, select only those constraints that prefer no losers = PNL
- Out of PNL, take just the Markedness constraints and install them at the bottom of the ranking
- If there are no Markedness constraints, select the smallest set of Faithfulness constraints that will "free up" a Markedness constraint at the next step
- Remove from consideration all winner-loser pairs that have a W mark for one of the freshly installed constraints


## Inconsistency

- BCD is dependent on constraints without $L$ marks
- When there are no such constraints, this means something's wrong
- Cues mutually inconsistent rankings, e.g., input 1 wants $A \gg B$, input 2 wants $B \gg A$ : mutually incompatible
- Pater (2010): when you encounter inconsistency, induce some indexed constraint
- Gets you out of inconsistency: input 1 wants $A i \gg B$, input 2 wants $B \gg A$ : mutually compatible!


## Indexed constraint selection

- Round (2017) wants model that infers segmentally local indices
- Therefore: violations track segment instances ("loci") *[+voice] has a W violation in the second " $b$ " for $W$-L pair 1, but a $L$ violation in the first " $v$ " for $W$ - $L$ pair 2
- For each constraint, compute:
- $\Phi_{\mathrm{w}}$ : Set of segment instances that get a W violation of that constraint
- $\Phi_{L}$ : Set of segment instances that get a $L$ violation of that constraint
- $\Phi_{W}-\Phi_{L}$ : Set of segment instances that get a $W$ violation but never a $L$ violation of that constraint


## Indexed constraint selection

- Round (2017) wants model that infers segmentally local indices
- For each constraint, compute:
- $\Phi_{\mathrm{w}}$ : Set of segment instances that get a W violation of that constraint
- $\Phi_{L}$ : Set of segment instances that get a $L$ violation of that constraint
- $\Phi_{W}-\Phi_{L}$ : Set of segment instances that get a $W$ violation but never a $L$ violation of that constraint
- Make [+i] indexed version of constraint that has the greatest $\Phi_{w}-\Phi_{L}$ :
- $\Phi_{\mathrm{W}}-\Phi_{\mathrm{L}}$ become [+i], all other segments instances become [-i] (binarity: AN)


## Restrictiveness

- Grammars were evaluated on whether they were potentially restrictive
- The consonants before which/ar,av/ raise are the same consonants that alternate with a voiceless segment
- Learner had no way of assigning the same index to two different indexed constraints
- Restrictiveness assessed by seeing if Raising constraint indexed to subset of segments indexed to *[+voice]

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